Deep (2)

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Outline

ConvNets as Deep Neural Networks for Vision

1. Neural Nets
2. Deep Convolutional Neural Networks
   • Basics for deep in images
MLP example: brute force connection

First Pb: Scalability
Large images => extremely large number of trainable parameters
MLP example: brute force connection

2d Pb: Stability of the representation

Expectation:
- Small deformation in the input space
  => similar representations
- Large (or unexpected) transfo in the input space
  => very dissimilar representations
MLP example: brute force connection

Stability: Invariance/Robustness to (local) shifting, scaling, and other forms of (small) distortions?
MLP example: brute force connection

Little or no invariance to shifting, scaling, and other forms of distortion
MLP example: brute force connection

154 input change from 2 shift left
77 : black to white
77 : white to black

@LeCun
MLP example: brute force connection

Scaling and other forms of distortions => same pb
Conclusion of MLP on raw data

Brute force connection of images as input of MLP NOT a good idea
  • No Invariance/Robustness of the representation because topology of the input data completely ignored
  • Nb of weights grows largely with the size of the input image

How keep spatial topology?
How to limit the weight number?
How to limit the weight numbers?

1/ Locally connected neural networks

- **Sparse connectivity**: a hidden unit is only connected to a local patch (weights connected to the patch are called filter or kernel)
- Inspired by biological systems, where a cell is sensitive to a small sub-region of the input space, called a receptive field. Many cells are tiled to cover the entire visual field
How to limit the weight numbers?

2/ Shared Weights

- Hidden nodes at different locations share the same weights
  - greatly reduces the number of parameters to learn
- Keep spatial information in a **2D feature map** (hidden layer map)

⇒ Computing responses at hidden nodes equivalent to convoluting input image with a linear filter (learned)
⇒ A learned filter as a feature detector
Convolution filters

unit impulse $\delta[n] = 1[n = 0]$

every signal $x$ expressed as

$$x[n] = \sum_k x[k] \delta[n - k] = \sum_k x[k] s_k(\delta)[n]$$

if $f$ is LTI with impulse response $h = f(\delta)$, then

$$f(x)[n] = f \left( \sum_k x[k] s_k(\delta) \right)[n] = \sum_k x[k] s_k(f(\delta))[n]$$

$$= \sum_k x[k] h[n - k] := (x * h)[n]$$
What does replicating the feature detectors achieve?

• Equivariant activities (Hinton Ex): Replicated features do not make the neural activities invariant to translation. The activities are equivariant.

⇒ How to get invariance to 2D spatial transformation of the input?
Getting local Invariance

3/ (local) spatial **POOLING** of the outputs of replicated feature detectors:

- Averaging neighboring replicated detectors to give a single output to the next level
- Max pooling: Taking the maximum in a neighboring

Get a small amount of **translational invariance** at each level
Reducing the number of inputs to the next layer of feature extraction

=> Stability OK (at least for local shift) for Convolutional Net!
Ex. of convolution operator and pooling operator

**Convolution**

\[
\begin{array}{cccc}
35 & 40 & 41 & 45 & 50 \\
40 & 40 & 42 & 46 & 52 \\
42 & 46 & 50 & 55 & 55 \\
48 & 52 & 56 & 58 & 60 \\
50 & 60 & 65 & 70 & 75 \\
\end{array}
\times
\begin{array}{cccc}
0 & 1 & 0 \\
0 & 0 & 0 \\
0 & 0 & 0 \\
\end{array}
= \begin{array}{c}
42 \\
\end{array}
\]

**Pooling (Subsample)**

local averaging operator

\[
y_{ij} = \frac{1}{4}(x_{2i,2j} + x_{2i+1,2j} + x_{2i,2j+1} + x_{2i+1,2j+1})
\]
From one to many filters

1 filter => 1 feature map (corresponding to 1 visual pattern)
To detect spatial distributions of multiple visual patterns: Multiple filters
M filters => M feature maps! Get richer description

E.g.: 1000x1000 image
100 Filters
Filter size: 10x10
10K parameters

Learn multiple filters.

Not a big deal!
Many filters
=> few parameters
From one to many filters

M filters => M feature maps
To sum up:

- \( M \) filters
- \( M \) feature maps

Diagram:

```
M filters

\[ \text{Convol.} \rightarrow \text{Pooling} \]

M feature maps
```
Color images: 3D kernels for filtering

$m \times n \times d$ parameters per filter
Idem for any layer $i$ to layer $i+1$
LCN: Local Contrast Normalization

Normalization within a neighborhood along both spatial and feature dimensions

\[ h_{i+1,x,y,k} = \frac{h_{i,x,y,k} - m_{i,N(x,y,k)}}{\sigma_{i,N(x,y,k)}} \]

\[ \text{Layer } i \quad \text{Layer } i+1 \]

=> Very important for training large nets to carefully consider normalization within mini-batches [S. Ioffe, C. Szegedy 2015]
1 stage of convolutional neural networks
1 stage of convolutional neural networks

A hidden unit in the first hidden layer is influenced by a small neighborhood (equal to size of filter).

Ranzato CVPR’13
A hidden unit after the pooling layer is influenced by a larger neighborhood (it depends on filter sizes and the sizes of pooling regions)
Full ConvNet architecture

One stage (zoom)

Convol.  LCN  Pooling

Whole system

Input Image

1st stage  2nd stage  3rd stage

Fully Conn. Layers

Class Labels
To sum up: Full ConvNet architecture
To sum up: Full ConvNet architecture

CNN: feed-forward network with
ability to extract topological properties from image

designed to recognize visual patterns

Working directly from pixel images with (no/minimal) preprocessing

Trained with back-propagation
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   1. Basics for deep in images
   2. One example: LeNet5
Example: LeNet5

Introduced by Y. LeCun

Raw image of 32 × 32 pixels as input
Example: LeNet5

- **C1, C3, C5**: Convolutional layer
- **$5 \times 5$ Convolution matrix**
- **S2, S4**: Subsampling layer = Pooling+stride $s=2$
  
  => Subsampling by factor 2
- **F6**: Fully connected layer
LeNet5

All the units of the layers up to F6 have a sigmoidal activation function
LeNet5

About 187,000 connections
About 14,000 trainable weights
LeNet5 (@LeCun)
LeNet5 (@LeCun)
Comparison BoW / deep CNN

- **Input image**
- **Convolution**
- **Sub-sampling**
- **Convolution**
- **Sub-sampling**
- **Fully-connected weights**
- **Class labels**

**Feature extraction (e.g. SIFT)**

- **Feature coding**
- **Max-pooling**
- **Classifier**

- **Local gradient coding**
- **Pooling**
- **Visual codes**
- **Image signature**
- **Class label**
Comparison BoW / CNN deep

1. Regular grid + gradient detection (SIFT) => bank of 8 linear filters (convolution) + Winner Take All (inter-maps) => 8 maps
2. Local histogram SIFT => spatial local sum pooling inside maps on a fixed grid 4x4 => 16x8=128 (smaller) maps
3. BoW Coding = projection on M vectors (visual dico elts) => a bank of M linear filters of size 4x4x8 (=1x1x128 convolution) => M maps
4. BoW Pooling => global pooling on each map => M scalar values = 1 vector representation BoW (extension: SPM)
5. Classification (SVM) => Fully connected layers

BoW = Conv1+pooling(loc)+Conv2+pooling(global)+Fconnected
- Handcrafted+unsupervised vs. end-to-end supervision
- Light deep vs. very deep
Deep vs shallow in Computer Vision

• CV work(ed) a lot on handcrafted local features
  • BoVW (Bag of Visual Words and extensions FisherVectors, BossaNova …)
  • BoVW not so shallow but not end-to-end supervised learning
• CNN: end-to-end learning on a **handcrafted** architecture! [Chatfield BMVC 2014]
  • Why 8 layers? why 3x3 at the 5th layer without polling? … => ad-hoc architecture
Zero-padding in convolutional neural network (optional)

To avoid shrinking the spatial extent of the network rapidly
Invariance to local translation (small shift) OK with pooling
Is convolution equivariant/invariant to changes in scale or rotation?
   No such invariance with linear filters
Possible extension:
   Pooling OVER outputs of separately parameterized convolutions
   Become possible to LEARN invariance to rotation (or other)
Example (Bengio et al. Deep Learning 2014):
By learning to have each filter be a different rotation of the “5” template +
pooling over outputs => invariance to rotation of the “5”

“This is in contrast to translation invariance, which is usually achieved by
hard-coding the net to pool over shifted versions of a single learned filter”